## Arc of Learning for Comparing Bits and Pieces

Rational numbers are at the heart of the middle-grades experience with number concepts. The goal of Comparing Bits and Pieces is to help students deepen their understanding of equivalent fractions and build on this understanding as they explore ratios. They will become skillful at interpreting the different forms of a rational number, at knowing which form is most appropriate for the solution of a given problem, and at writing and interpreting ratios.

| Comparing Bits and Pieces: Ratios, Rational Numbers, and Equivalence |  |  |  |  |  |
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| Equivalent Fractions | Introduction Setting the Scene | Exploration Mucking About | Analysis Going Deeper | Synthesis Looking Across | Abstraction Going Beyond |
| Investigation 1: Making Comparisons |  |  |  |  |  |
| 1.1 Fundraising: Comparing With Fractions and Ratios | 1.1 |  |  |  |  |
|  | 1.1 |  |  |  |  |
| 1.2 Fundraising Thermometers: Introducing Ratios | 1.2 | 1.2 |  |  |  |
|  | 1.2 | 1.2 |  |  |  |
| 1.3 Equivalent Fractions on the Line |  | 1.3 |  |  |  |
| 1.4 Measuring Progress: Finding Fractional Parts |  | 1.4 |  |  |  |
| 1.5 Comparing Fundraising Goals: Using Fractions and Ratios |  | 1.5 |  |  |  |
|  |  | 1.5 |  |  |  |
| Mathematical Reflections |  | MR |  |  |  |
|  |  | MR |  |  |  |
| Investigation 2: Connecting Ratios and Rates |  |  |  |  |  |
| 2.1 Equal Shares: Introducing Unit Rates |  |  |  |  |  |
|  |  | 2.1 |  |  |  |
| 2.2 Unequal Shares: Using Ratios and Fractions |  | 2.2 | 2.2 |  |  |
|  |  | 2.2 |  |  |  |
| 2.3 Making Comparisons with Rate Tables |  |  | 2.3 |  |  |
|  |  | 2.3 | 2.3 |  |  |
| Mathematical Reflections |  |  | MR |  |  |
|  |  | MR |  |  |  |
| Investigation 3: Extending the Number Line |  |  |  |  |  |
| 3.1 Extending the Number Line: Integers and Mixed Numbers |  |  | 3.1 |  |  |
|  |  |  |  |  |  |
| 3.2 Estimating and Ordering Rational Number: Comparing Fractions to Benchmarks |  |  | 3.2 |  |  |
|  |  |  |  |  |  |
| 3.3 Sharing 100 Things: Using Tenths and Hundredths |  |  | 3.3 |  |  |
| 3.4 Decimals on the Number Line |  |  | 3.4 |  |  |
| 3.5 Earthquake Relief: Moving From Fractions to Decimals |  |  | 3.5 |  |  |
|  |  | 3.5 |  |  |  |
| Mathematical Reflections |  |  | MR |  |  |
| Investigation 4: Working with Percents |  |  |  |  |  |
| 4.1 Who Is the Best? Making Sense of Percents |  |  |  | 4.1 |  |
|  |  | 4.1 |  |  |  |
| 4.2 Genetic Traits: Finding Percents |  |  |  | 4.2 |  |
|  |  | 4.2 |  |  |  |
| 4.3 The Art of Comparison: Using Ratios and Percents |  |  |  | 4.3 |  |
|  |  | 4.3 | 4.3 |  |  |
| Mathematical Reflections |  |  |  |  |  |
|  |  | MR |  |  |  |
| Looking Back |  |  |  | LB | LB |
|  |  | LB | LB |  |  |

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